

## References for the Guiding Principles Mathworks Curriculum Project

### 1. *Doing mathematics* is about making sense of and thinking deeply about fundamental concepts.

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## 2. **Persistence** is critical to success in problem-solving and doing mathematics

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3. Teachers need to establish a **classroom culture** that develops students' curiosity and imagination

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