Across the River...and
Through the Mountains...
See Page 4
Descartes

by Hiroko Warshauer

Hiroko Warshauer teaches mathematics at Southwest Texas State University. She enjoys music and the arts, as well as working with students on math puzzles, problems, and activities.

Have you ever wanted to stay in bed a little longer in the mornings? Here's one mathematician who often did and who came up with some great mathematical and philosophical ideas from the horizontal position!

A truly outstanding achievement credited to Descartes (pronounced "day-cart") is the connection he made between algebra, the language and words, and geometry, the pictures. The study of coordinate geometry and analytic geometry allows us to talk about points, lines, and curves with corresponding "addresses" or equations. More about this in the article on page 3.

Rene Descartes was born in France on March 31, 1596. At age eight he was sent to a Jesuit school, where he studied the classics (Greek and Latin literature) and gentlemanly behavior. Young Descartes' health was very delicate. For most of his life, Descartes would spend his morning hours in bed contemplating mathematics and philosophy. He left the school eight years later and spent a few years seeing the world and learning about life. In those years, Descartes also earned a law degree and began his work in mathematics and philosophy.

In 1617, at the age of 21, Descartes enlisted as a soldier, serving in the Dutch army and later in the Bavarian army until 1628. Afterwards, he lived in the Netherlands for 20 years. It was during those years in the Netherlands that Descartes published La Geometrie, his only mathematical work and other articles on his philosophical ideas. A well-known Latin phrase that is credited to Descartes, "cogito ergo sum" means "I think therefore I am." So the next time you are hurried out of bed you can say that you were thinking deeply like the famous philosopher Descartes.

The Cartesian Coordinate System

by Hiroko Warshauer

Finding the location of a building in an unfamiliar city can be difficult without knowing its address. Luckily for us, most cities and towns give homes and buildings addresses. Addresses help mail carriers, fire fighters, and mapmakers (cartographers) locate places in a city.

In mathematics, the geometric shapes such as lines, circles, and curves, made up of infinitely many points, can be related to a mathematical statement or equation that refers to the coordinates or addresses of the points. The sixteenth century mathematician and philosopher Rene Descartes (see page 2) came up with an amazing but simple idea. The location of a point in a plane (a flat surface) can be described using a pair of numbers. The numbers indicate the distance and direction from a pair of lines.

Let's begin with one line, namely the number line. We'll call this the x-axis or the horizontal axis. The number line has a number or coordinate associated to every point. For example, point A has coordinate 3 and point B has coordinate -3. Coordinates are like addresses for points.

Take another number line, this one vertical, and place it over the first so that they cross at the points labeled 0. We call this vertical line the y-axis or vertical axis. The intersection point is called the origin.

In this layout, called a rectangular coordinate system (or Cartesian coordinate system, after Descartes), each point is given an address consisting of two numbers called coordinates. For example, point P in the graph below marks the location of an Easter egg that has coordinates (1,2). Let's see why this might make sense.

In order to get to our point P, we could begin at the origin and first go 1 unit to the right along the x-axis. We could then go 2 units up along the y-axis. The first coordinate, 1, tells us how many units to go left or right along the x-axis. The second coordinate, 2, tells us how many units to go up or down. We can then use the coordinates to locate our points.

Can you write the pair of coordinates for the points above which mark the location of the Easter eggs?

R has coordinates (____, ___)
S has coordinates (____, ___)
T has coordinates (____, ___)
PROBLEMS OF THE MONTH

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1. Draw a grid to locate points in the Cartesian plane.
   Locate the point (2,3). Find as many points as you can that are a distance of 4 units from the point (2,3).

2. Use your grid above to draw a line from (-4,6) to (6,-2). What point on this line is midway between these two points?

3. A number whose value is the same read forward and backwards is called a palindrome. One such number is 121. How many palindromes are there between 100 and 200?

4. What is the sum of the digits of the palindrome closest to 1999?

5. Sandy puts some slices of cake on the table. If she puts out 8 more slices then she and her 4 friends will be able to have 3 slices each. How many slices did she put out on the table in the beginning?

6. King Pancake ordered 77 pancakes from his chef for dinner. The chef can make 5 pancakes in 1 minute, but every time he makes 5 new pancakes, 4 pancakes mysteriously disappear. Under these circumstances, how long does it take the chef to make the 77 pancakes?

7. Ingenuity Terry would like to visit Diann who lives over the river and behind the mountain. There are 5 bridges over the river and 3 tunnels through the mountain. As you can see in the picture, there is a fence between the river and the mountain which Terry cannot climb over. How many different paths can Terry take to get to Diann if he can cross every bridge only once?
What is the largest number you can think of? (Here I am asking about actual counting numbers, not “infinity”.) People answer this question in different ways depending on how many numbers they know. Preschoolers might answer “one hundred” because that is how far they have learned to count. Others might answer with a “zillion” or a “skillion” or (my favorite) an “impossibillion”. But these names are not really defined—they are not standard names for any numbers.

When I first learned about large numbers (a large number of years ago), I read about a “googol”. This nonsense name was made up to represent the number

\[100000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000000\]

This is one followed by one hundred zeros. It is a very big number. If the entire visible universe were packed solid with atoms, there would be fewer than a googol atoms there.

The name “googol” was invented around 1940 by E. Kasner and J. R. Newman. They also defined a googolplex to be the number which is a one followed by a googol zeros. Writing out a googolplex in the usual base ten notation would take up a lot of time and paper. In fact, there isn’t enough paper on earth to do it!

Here is a more compact way to write such large numbers. If b and n are whole numbers then \(b^n\) (read “b to the n”) is the product of b times itself, n times. For example,

\[5^2 = 5 \times 5 = 25\]
\[3^4 = 3 \times 3 \times 3 \times 3 = 81\]
\[10^2 = 10 \times 10 = 100\]
\[10^3 = 10 \times 10 \times 10 = 1000\]

From these examples you can see that \(10^n\) is exactly the number which is a one followed by n zeros. In particular, a googol is \(10^{100}\). Similarly a googolplex equals

\[10^{\text{googol}} = 10^{(10^{100})} = \text{(one googolplex)}\]

This is certainly a shorter way to write that number. Even though a googolplex is almost inconceivably large, there are other numbers so large that a googolplex seems small in comparison. In fact, most whole numbers are larger than a googolplex! (Does that seem right to you?) Can you use our shorthand notation to write down 3 numbers larger than a googolplex?

Numbers like a googol and a googolplex are ridiculously large compared to those we encounter in the real world. But in mathematics there are no limits to what we can describe with our imagination.

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Forwards or backwards, up, slanted, or down. Where can the words in this puzzle be found?

POINT
S S E L A N G H E M S B
CARTESIAN
W A D G I T I N E E M A T
PLANE
L P R O S P L A N E L S D R
DISTANCE
I A O M M U I A U D O M A I
DESCARTES
N S E N I S A E H E I R K J
PAIR
T L V O E C L V Q A N Q B M
NUMBER
E C T R E A N G L S E A I N
LINE
V A R T T C I C E C A U R U
SUM
R E R E B E C N A T S I D M

THE SMALLEST WALL
Write different positive whole numbers in the rectangles so that the sum of two neighboring numbers is in the rectangle above them and the number on top is the smallest possible.

THE WALL GAME
Fill in the empty rectangles so that the sum of two neighboring numbers is in the rectangle above them.

a)

10 20 30 40

b)

90

40

60

c)

45

80

17

55

144

24

48

3

9

15

6
More Fun Problems

One place to find fun problems is on the web. Xingde Jia has weekly problems and projects that kids can work on. Check it out at http://erdos.math.swt.edu/contest

His students at the Austin Great Wall Chinese School are pictured below.

X

Xingde Jia, Professor of Mathematics at Southwest Texas State University volunteers to teach a Sunday math class at the Austin Great Wall Chinese School. Pictured to the right are his students.

T

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Answer to Riddle: At 11 PM at night.