

Po Leung Kuk 9th Primary Mathematics World Contest

Group Contest 2005

Team: _____

Question 1:

Call an integer “happy”, if the sum of its digits is 10. How many “happy” integers are there between 100 and 1000?

Ans: _____

Question 2:

Compute the sum of a , b and c given that $\frac{a}{2} = \frac{b}{3} = \frac{c}{5}$ and the product of a , b and c is 1920.

Ans: _____

Question 3:

Replace the letters a , b , c and d in the following expression with the numbers 1, 2, 3 and 4, without repetition:

$$a + \frac{1}{b + \frac{1}{c + \frac{1}{d}}}$$

Find the difference between the maximum value and the minimum value of the expression.

Ans: _____

Question 4:

Buses from town A to town B leave every hour on the hour

(for example: 6:00, 7:00, ...).

Buses from town B to town A leave every hour on the half hour

(for example: 6:30, 7:30, ...).

The trip between town A and town B takes 5 hours. Assume the buses travel on the same road.

If you get on a bus from town A, how many buses from town B do you pass on the road (not including those at the stations)?

Ans: _____

Question 5:

Mr. Wong has a 7-digit phone number ABCDEFG. The sum of the number formed by the first 4 digits ABCD and the number formed by the last 3 digits EFG is 9063. The sum of the number formed by the first 3 digits ABC and the number formed by the last 4 digits DEFG is 2529. What is Mr. Wong's phone number?

Ans: _____

Question 6:

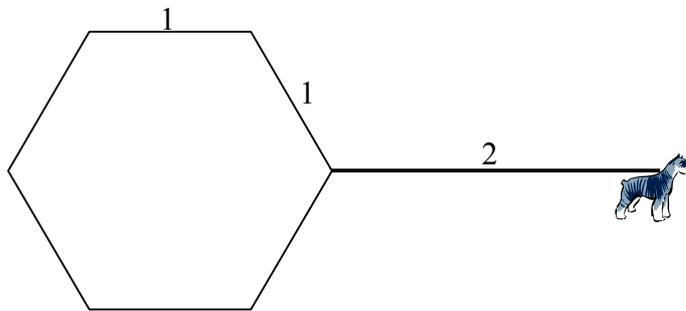
$$\begin{aligned}1 + 2 &= 3 \\4 + 5 + 6 &= 7 + 8 \\9 + 10 + 11 + 12 &= 13 + 14 + 15 \\&\vdots\end{aligned}$$

If this pattern is continued, find the last number in the 80th row
(e.g. the last number of the third row is 15).

Ans: _____

Question 7:

Skipper's doghouse has a regular hexagonal base that measures one metre on each side. Skipper is tethered to a 2-metre rope which is fixed to a vertex. What is the area of the region outside the doghouse that Skipper can reach? Calculate an approximate answer by using $\pi = 3.14$ or $22/7$.

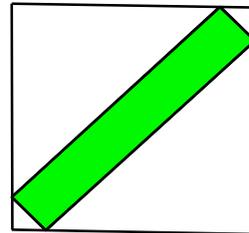


Ans: _____m²

Question 8:

An isosceles right triangle is removed from each corner of a square piece of paper so that a rectangle of unequal sides remains.

If the sum of the areas of the cut-off pieces is 200 cm^2 and the lengths of the legs of the triangles cut off are integers, find the area of the rectangle.



Ans: _____ cm^2

Question 9:

Select 8 of the 9 given numbers: 2, 3, 4, 7, 10, 11, 12, 13, 15 and place them in the vacant squares so that the average of the numbers in each row and column is the same. Complete the following table.

| | | | |
|---|---|----|---|
| 1 | | | |
| | 9 | | 5 |
| | | 14 | |

Ans: _____

Question 10:

Find the largest 12-digit number for which every two consecutive digits form a distinct 2-digit prime number.

Ans: _____